

## Useful mathematical vocabulary

<b>+</b>	
plus	more
altogether	combine
total	add
makes	increase
and	count on
sum of	

<b>-</b>	
take away	difference
minus	subtract
count back	how many left?
leaves	less
decrease	

<b>x</b>	
repeated addition	multiply
groups of	product
lots of	pairs
times	double

<b>÷</b>	
share	share equally
divide	divisible
group	divided by
split	

<b>=</b>	
is the same as	makes
totals	balances
equals	



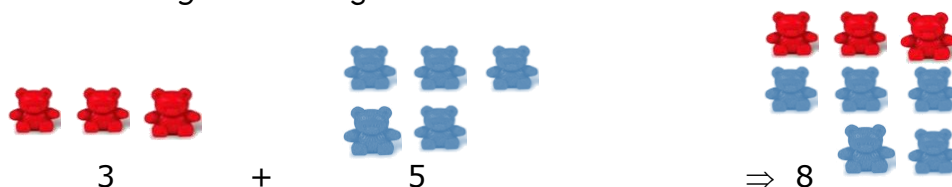
## Addition

### Stage 1

Count all

$$3 + 5$$

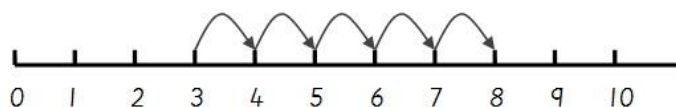
Count out three counters and then five counters and then find the total by counting all the counters.



Count on from the first number

$$3 + 5$$

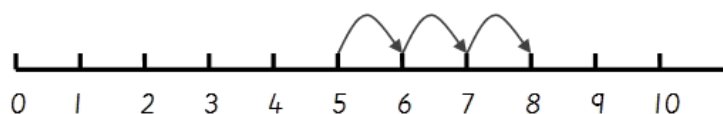
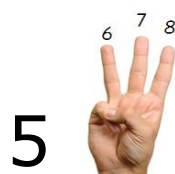
Count on from the first number: 'four, five, six, seven, eight'.



Count on from the larger number

$$3 + 5$$

Count on from the larger number: 'six, seven, eight'.



Count on from the larger number

$$35 + 23$$

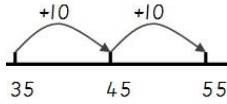
Count on 2 tens, then 3 units

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

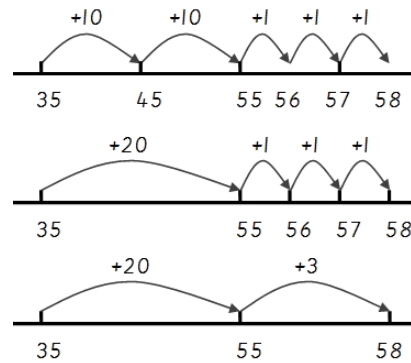
## Stage 2

### Counting on - number line

$$35 + 20$$



$$35 + 23$$



### Partitioning

Partition the number into tens and units. Add the tens, then the units.

$$\begin{array}{r}
 30 + 20 = 50 \\
 5 + 3 = 8 \\
 \hline
 50 + 8 = 58
 \end{array}$$

### Expanded Addition

To understand the value of each digit, partition the number and place them into columns.

$$\begin{array}{r}
 40 + 7 \\
 70 + 6 \\
 \hline
 110 + 13 = 123
 \end{array}$$

## Stage 3

### Compact Addition

$$\begin{array}{r}
 3587 \\
 675 \\
 \hline
 4262 \\
 \hline
 | \quad | \quad |
 \end{array}$$

$$\begin{array}{r}
 6584 \\
 5844 \\
 \hline
 12428 \\
 \hline
 | \quad |
 \end{array}$$

$$\begin{array}{r}
 3.68 \\
 4.23 \\
 \hline
 7.91 \\
 \hline
 |
 \end{array}$$

## Subtraction

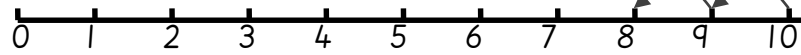
### Stage 1

Counting back (take away)

$10 - 5$

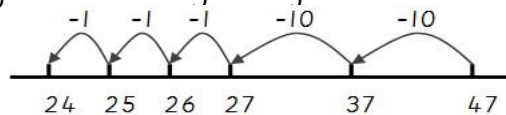


2 less than 10



How many have we got left?

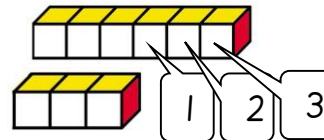
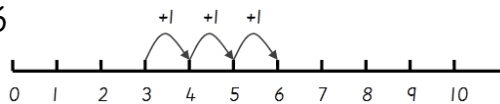
$47 - 23$



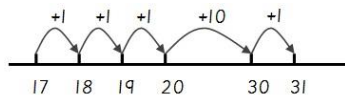
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Counting on (find the difference)

The difference between  
3 and 6



$31 - 17$



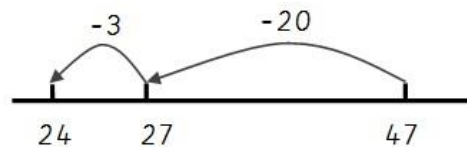
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Start at 17 and count on to 31

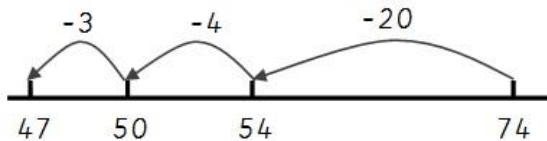
### Stage 2

Counting Back

$47 - 23$

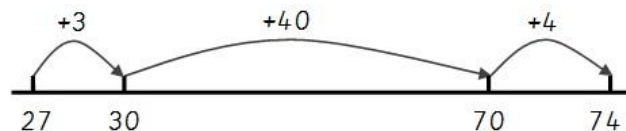


$74 - 27$

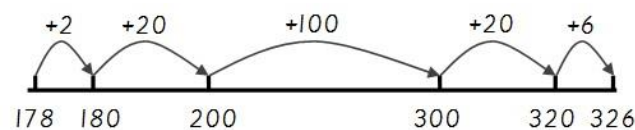


Counting On (find the difference)

$74 - 27 = 47$



$326 - 178 = 148$



**Partitioning**

$$58 - 23 = 35$$

$$74 - 27 = 47$$

$$58 - 20 = 38$$

$$74 - 20 = 54$$

$$38 - 3 = 35$$

$$54 - 7 = 47$$

**Expanded Method**

$$\begin{array}{r}
 47 - 23 \\
 40 \text{ and } 7 \\
 20 \text{ and } 3 \\
 \hline
 20 \text{ and } 4 \\
 =24
 \end{array}$$

$$\begin{array}{r}
 182 - 57 \\
 100 \quad \cancel{7}0 \quad 12 \\
 \quad \quad 50 \quad 7 \\
 \hline
 100 \quad 20 \quad 5 \\
 =125
 \end{array}$$

**Stage 3**

**Compact method (with decomposition)**

974 - 548      4 is less than 8  
EXCHANGE a ten for 10 new units and add these to the 4 to make 14.  
 Remember to change the 70 to 60.

$$\begin{array}{r}
 9 \overset{6}{\cancel{7}} \overset{1}{4} \\
 548 \\
 \hline
 426
 \end{array}$$

5809 - 2634      EXCHANGE a hundred for 10 new tens and add these to make 100 - 30.  
 Remember to change the 800 to 700

$$\begin{array}{r}
 5 \overset{7}{\cancel{8}} \overset{1}{0} 9 \\
 2634 \\
 \hline
 3175
 \end{array}$$

£73.79 - £45.55

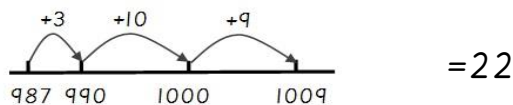
$$\begin{array}{r}
 \overset{6}{\cancel{7}} \overset{1}{3} . 79 \\
 \underline{\quad 45.55} \\
 \quad 28.24
 \end{array}$$

EXCHANGE a thousand, a hundred and a ten in this example.

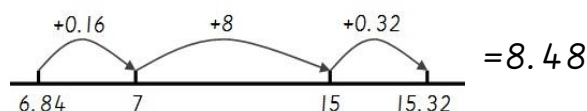
$$\begin{array}{r}
 \overset{6}{\cancel{7}} \overset{9}{\cancel{0}} \overset{9}{\cancel{1}} \overset{1}{2} \\
 \underline{\quad 1427} \\
 \quad 5575
 \end{array}$$

**Counting On**

$$1009 - 987$$



$$15.32 - 6.84$$



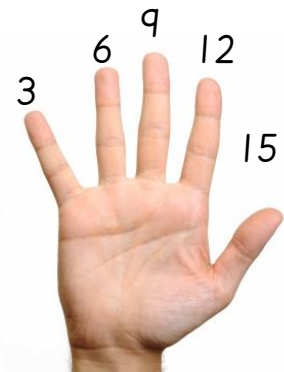
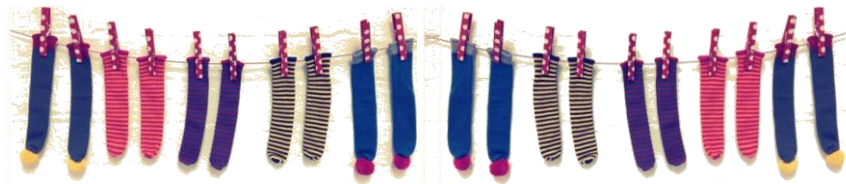
# Multiplication

## Stage 1

### Counting in equal steps

2s, 3s, 4s & 5s

2 4 6 8 10 12 14 16 18 20



### Repeated addition

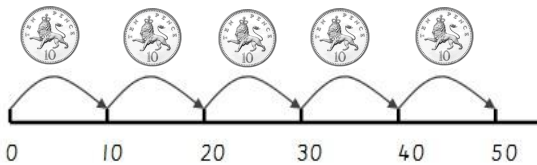


$$2 + 2 + 2 + 2 + 2 = 10$$

$$2 \times 5 = 10$$

2 multiplied by 5

5 pairs

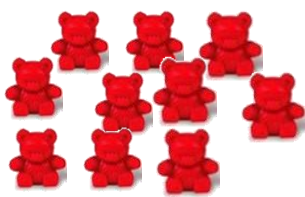


$$10p + 10p + 10p + 10p + 10p = 50p$$

$$10p \times 5 = 50p$$

5 jumps of 10

### Doubling numbers



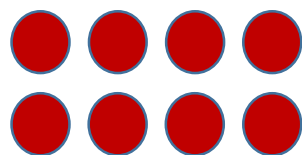
+



= 20

Double 10 equals 20

### Describing an array



$$4 \times 2 = 8$$

$$2 \times 4 = 8$$

## Stage 2

### Partitioning

$$36 \times 4 = 144$$

$$\begin{array}{r} 30 \times 4 = 120 \\ + \\ 6 \times 4 = \underline{24} \\ \hline 124 \end{array}$$

### Grid Method

$$38 \times 7 = 266$$

x	30	8	
7	210	56	

210	+	56
266		

$$284 \times 3 = 852$$

x	200	80	4	
3	600	240	12	

600	+	240	+	12
852				

## Stage 3

### Grid Method

$$56 \times 27$$

x	50	6	
20	1000	120	1120
7	350	42	392
			1512
			<u>1</u>

$$5.65 \times 9$$

x	5	0.6	0.05	
9	45	5.4	.45	
				45.00
				5.40
				<u>0.45</u>
				50.85

### Short Multiplication

$$28 \times 4$$

$$\begin{array}{r} 28 \\ \underline{4} \times \\ 32 \quad (8 \times 4) \\ \underline{80} \quad (20 \times 4) \\ \hline 112 \\ \underline{1} \end{array}$$

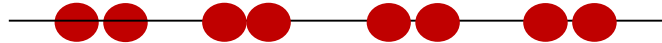
$$\begin{array}{r} 28 \\ \underline{4} \times \\ 112 \\ \underline{3} \end{array}$$

## Division

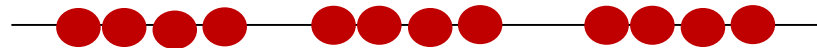
### Stage 1

Number tracks/Number lines

$$8 \div 2 = 4$$



$$12 \div 4 = 3$$



Halving numbers to 20

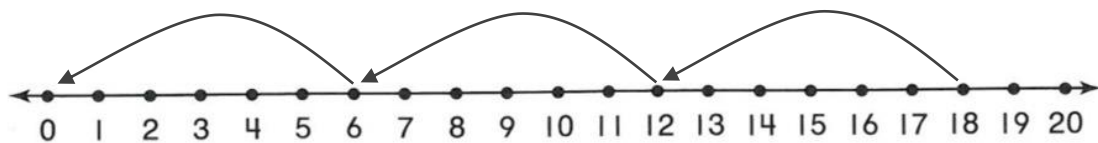
8 cakes shared between 2 plates



### Stage 2

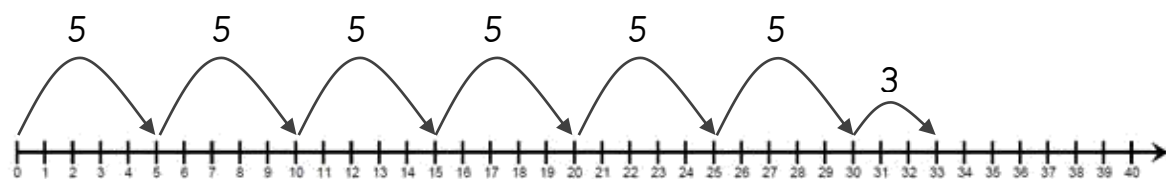
Number lines

$$18 \div 6 = 3$$



Number lines

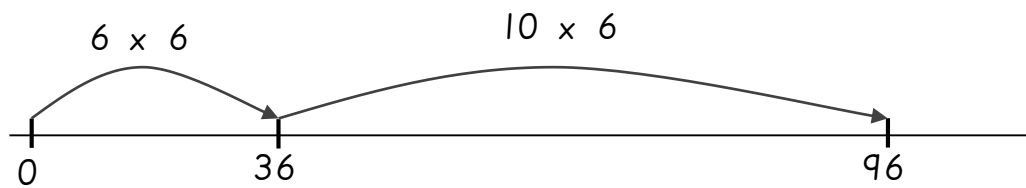
$$33 \div 5 = 6 \text{ r}3$$





Number lines

$$96 \div 6 = 16$$



**Stage 3**

Grouping (vertical layout)

$$96 \div 7 = 16$$

$$\begin{array}{r} 96 \\ \underline{70} \phantom{0} \\ 26 \\ \underline{21} \phantom{0} \\ 5 \end{array} \quad \begin{array}{l} (7 \times 10) \\ (7 \times 3) \end{array}$$

Answer: 13 r5

Grouping (expanded)

$$\begin{array}{r} 6 \overline{)196} \\ \underline{60} \phantom{0} \\ 136 \\ \underline{60} \phantom{0} \\ 76 \\ \underline{60} \phantom{0} \\ 16 \\ \underline{12} \phantom{0} \\ 4 \end{array} \quad \begin{array}{l} 6 \times 10 \\ 6 \times 10 \\ 6 \times 10 \\ 6 \times 2 \end{array}$$

'Empty' number line (start from 0) may be used to record calculation strategy

Answer 32 r4

Short Division

$$291 \div 3 \text{ (estimate: } 270 \div 3 = 90)$$

$$\begin{array}{r} 97 \\ 3 \overline{)291} \end{array}$$